

ปัจจัยที่มีผลต่อประสิทธิภาพการทำสารละลายแท้และสารละลายคงคลอยด์ให้เข้มข้น  
ด้วยวิธีแข็งแบบก้าวหน้า

นาง ประภาศรี เทพรักษา

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FACTORS AFFECTING THE EFFICIENCY OF THE PROGRESSIVE FREEZE-CONCENTRATION OF  
TRUE AND COLLOIDAL SOLUTION

Mrs. Prapasri Theprugsa

คุณย์วิทยาลัยการ

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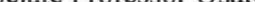
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งานวิจัยนี้ศึกษาวิธีการทำสารค่าสัมประสิทธิ์การแยกสูงสุด (Limiting Partition Coefficient;  $K_o$ ) และปัจจัยที่เกี่ยวข้องในการทำสารละลายให้เข้มข้นด้วยวิธีการแข็งเยือกแข็งแบบก้าวหน้า ค่า  $K_o$  สามารถหาได้จากค่าสัมประสิทธิ์การแยก (Effective Partition Coefficient,  $K$ ) ซึ่งได้จากการทดลองโดยตรง โดยอาศัยหลักการของแบบจำลองของปรากฏการณ์ concentration polarization ที่เกิดขึ้นที่ผิวน้ำระหว่างวัสดุค่าน้ำแข็งและของเหลว

ตัวแปรที่ทำการศึกษาได้แก่ อัตราการกวนที่ผิวน้ำแข็ง ในช่วง 200-1000 รอบต่อนาที อัตราการเคลื่อนตัวของผิวน้ำแข็ง ในช่วง 0.1-2.7 ซม./ชม ชนิดของสารละลาย ซึ่งประกอบด้วยสารละลายมีชื่อ ได้แก่ LiCl, NaCl, KCl และ CsCl สารละลายไม่มีชื่อ ได้แก่ ไฮโปโซ กลูโคส พรูโคโนส โซโนครอส และแลคโตส และสารละลายคอลloid ได้แก่ เดกซ์เตวน ที่มีน้ำหนักโมเลกุล 9,000-2,000,000 และ ความเข้มข้นเริ่มต้นของสารละลาย ( $C_0$ ) เท่ากับ 0.5-20% (w/w) ผลการศึกษาสำหรับสารละลายมีชื่อพบว่า ค่า  $K_o$  เป็นสัดส่วนโดยตรงกับความเข้มข้นเริ่มต้น และ ขึ้นกับชนิดของสารละลาย โดยที่  $K_o/C_0$  มีความสัมพันธ์เป็นเส้นตรงกับค่า Hydration Number ของอ่อนนุ่มในสารละลายซึ่งมีลำดับจากมากไปน้อยดังนี้ Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup> และ Cs<sup>+</sup> สารละลายไม่มีชื่อให้ผลแบบเดียวกับสารละลายมีชื่อ แต่ค่า  $K_o$  ของสารละลายมีชื่อจะไม่ขึ้นกับชนิดของตัวถูกละลาย สำหรับสารละลายคอลloid นั้น ไม่พบว่าค่า  $K_o$  ขึ้นกับขนาดโมเลกุล และความเข้มข้นเริ่มต้นของสารละลาย

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KEY WORD: progressive freeze-concentration / effective partition coefficient / limiting partition coefficient / ice crystal growth rate /

PRAPASRI THEPRUGSA : FACTORS AFFECTING THE EFFICIENCY OF THE PROGRESSIVE FREEZE-CONCENTRATION OF TRUE AND COLLOIDAL SOLUTION.

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In this research, the limiting partition coefficients ( $K_o$ ) were determined. Factors affecting the progressive freeze concentration process were also investigated.  $K_o$  could be obtained from the effective partition coefficient ( $K$ ), which was, in turn, obtained experimentally using the concentration polarization model.

The factors studied in this research included the stirring speed at the ice-liquid interface, in the range of 200-1000 rpm; the advance rate of the ice front, in the range of 0.1-2.7 cm/h; and the type of solution, which included ionic solutions comprising LiCl, NaCl, KCl, and CsCl, non-ionic solutions comprising ribose, glucose, fructose, sucrose, and lactose; and colloidal solutions comprising dextran with the molecular weight ranging from 9,000-2,000,000 and the initial concentration ranging from 0.5-20% (w/w). It was found that, for the ionic solutions the  $K_o$  value depends directly on initial concentration ( $C_0$ ) and type of solution. It was also found that the  $K_o/C_0$  ratio was linearly proportional to the hydration number of the cation of the solute, which could be ordered as follows: Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup>, Cs<sup>+</sup>. For the non-ionic solutions, the results were similar to those of the ionic solutions, except that the  $K_o$  value was not affected by the type of the solute. The  $K_o$  value of the colloidal solution (i.e. dextran) was found that to be not affected by the size of molecule and the initial concentration of the solution.

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