

บรรณานุกรม

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#### วิทยานิพนธ์

- คู่กล้า ธรรมรักษา. "การศึกษาเปรียบเทียบวิธีการประมาณค่าแวนเรียนซ์คอมโพเนนท์ ใน แผนแบบไม่สมดุลย์ในกรณีการแจกแจงแบบสองทาง." วิทยานิพนธ์ปริญญามหาบัณฑิต ภาควิชาสถิติ บัณฑิตวิทยาลัย จุฬาลงกรณ์มหาวิทยาลัย, 2524.



ภาคผนวก

ศูนย์วิทยทรัพยากร  
จุฬาลงกรณ์มหาวิทยาลัย



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.....
C.....
C.....          PROGRAM PROCESS
C.....          =====
C.....
C.....          1. GENERATE RANDOM NUMBER WITH UNIFORM DISTRIBUTION
C.....          2. GENERATE DATA WITH NORMAL DISTRIBUTION
C.....              MEAN          =          ZERO
C.....              STANDARD DEVIATION =          SIGMA
C.....          3. GENERATE DATA WITH 2-WAY CLASSIFICATION
C.....              AND UNBALANCED DESIGN
C.....              RANDOM MODEL:
C.....
C.....              Y      =  U + A  + B  + AB  + E
C.....              IJK      I      J      IJ      IJK
C.....
C.....          4. ESTIMATE VARIANCE COMPONENT BY 4 METHOD :
C.....              4.1 ANOVA METHOD
C.....              4.2 ML METHOD WITH ANOVA AS PRIOR
C.....              4.3 MINVQUE METHOD WITH ANOVA AS PRIOR
C.....              4.4 I-MINVQUE METHOD BY ITERATING MINVQUE
C.....          5. CALCULATE MSE(ESTIMATOR) OF EACH METHOD IN 4.
C.....
.....
C
C          VARIABLES DESCRIPTION
C          =====
C
C          VARIABLES          DESCRIPTION
C          =====
C
C  ISEED1          SEED FOR GENERATE A-EFFECT      ==> 973253
C  ISEED2          SEED FOR GENERATE B-EFFECT      ==> 876541
C  ISEED3          SEED FOR GENERATE AB-EFFECT     ==> 778467
C  ISEED4          SEED FOR GENERATE E-EFFECT      ==> 392485
C  MEANS          MEAN OF EACH EFFECT             ==> 0
C  MEAN          GRAND MEAN
C  KOUNT1         NC. OF REPEAT SIMULATION = 200 TIMES
C  SMSE(I)       SUM OF MSE(ESTIMATOR) SQUARE IN I-TH METHOD
C  MSE(I,J)      MEAN SQUARE ERROR OF J-TH VARIANCE COMPONENT
C               ESTIMATOR IN THE J-TH METHOD
C  SS(I,J)       SUMMATION OF (ESTIMATOR-PARAMETER) * * 2
C               IN THE J-TH COMPONENT AND I-TH METHOD
C  LI           NC. LEVEL OF FACTOR A
C  LJ           NC. LEVEL OF FACTOR B
C  NC(I,J)      NC. OF OBSERVATION IN CELL (I,J)
C  SIGMA(I)     STANDARD DEVIATION OF THE I-TH COMPONENT
C  U1(I,J)      I*J MATRIX OF COEFFICIENT OF A-EFFECT
C  U2(I,J)      I*J MATRIX OF COEFFICIENT OF B-EFFECT
C  U3(I,J)      I*J MATRIX OF COEFFICIENT OF AB-EFFECT
C  V1(I,J)      I*J MATRIX OF U1*U1-TRANSPCST
C  V2(I,J)      I*J MATRIX OF U2*U2-TRANSPCST
C  V3(I,J)      I*J MATRIX OF U3*U3-TRANSPCST
C  V4(I,J)      IDENTITY MATRIX
C  V(I,J)       I*J MATRIX OF SUMMATION OF SIGMA SQUARE *
C               U * U-TRANSPCST
C  VE(I,J)      I*J MATRIX OF VARIANCE J-TH COMPONENT ESTIMATOR
C               OF I-TH METHOD
C  VIN(I,J)     I*J MATRIX OF V-INVERT
C  X(I)         VECTOR OF 1
C  Y(I)         VECTOR OF OBSERVATION
C  Y(I,J,K)     OBSERVATION VALUE AT THE I-TH LEVEL OF A-FACTOR ,
C               J-TH LEVEL OF B-FACTOR AND K-TH VALUE OF CELL (I,J)
C  ALPHA(I)     RANDOM EFFECT OF THE I-TH LEVEL OF FACTOR A
C  BETA(J)      RANDOM EFFECT OF THE J-TH LEVEL OF FACTOR B
C  DINTRC(JI)   RANDOM EFFECT OF THE I-TH, J-TH INTERACTION AB
C  EFFCR(I)     RANDOM EFFECT OF ERROR
C  EFFECTA(I)   EFFECT OF FACTOR A IN THE I-TH LEVEL
C  EFFECTB(J)   EFFECT OF FACTOR B IN THE J-TH LEVEL
C  DINTRE(JI)   EFFECT OF INTERACTION AB
C  C(I)         DUMMY VECTOR
C  F(1)         "
C  F(I)         "
C  IROW(I)      "
C  ICOL(I)      "

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C
C-----C
C
C  SUBROUTINE
C  =====
C
C  MINV          SUBROUTINE FROM IBM USER GUIDE TO FIND INVERT
C                MATRIX AND DETERMINANT
C  GPFDD        SUBROUTINE FROM IBM USER GUIDE FOR MULTIPLY MATRIX
C  MFGF         SUBROUTINE FROM IBM USER GUIDE TO FIND RANK OF
C                MATRIX
C  TRACE        SUBROUTINE TO FIND TRACE OF MATRIX
C  RANDU        SUBROUTINE TO GENERATE RANDOM NUMBER WITH UNIFORM
C                DISTRIBUTION
C
C-----C
C
C  FUNCTION
C  =====
C
C  NCRM          FOR GENERATING DATA WITH NORMAL DISTRIBUTION
C
C-----C
C
C  DIMENSION NC(6,6),J1(30,6),U2(30,6),L3(30,36),V1(30,30),
1  V2(30,30),V3(30,30),V4(30,30),V(30,30),Y(30),X(30),
2  VIN(30,30),YSX(30),VV1(30,30),VV2(30,30),VV3(30,30),
3  VV4(30,30),VE(4,4),S(4),TR(4,4),IRGW(30),ICCL(30),C(900),
4  E(900),F(900),VJV1(30,30),VR(4),C(30,30),XVXI(1),VA(4,4),
5  SS(4,4),SIGMA(4),SIGMAS(4),ALPHA(6),BETA(6),DINTRC(6),
6  ERROR(30),EFECTA(30),EFECTB(30),DINTER(30),Y1(6,6,30),
7  TTA(6),TTB(6),TTAB(6,6),NJ(6),NJ(6),P(3,3),SMSE(4)
C
C-----C
C
C  REAL MSE(4,4),MEAN,NORM,LIKH,MAX
C
C-----C
C
C  ISEED1 = 973253
C  ISEED2 = 876541
C  ISEED3 = 778467
C  ISEED4 = 392485
C  MEANS = 0
C  MEAN = 0
C  KOUNT1 = 0
C  DO 111 I = 1,4
C  SMSE(I) = 0
C  DO 111 J = 1,4
111  SS(I,J) = 0
C  READ(5,1114) (SIGMAS(I),I=1,4),CV
C  READ(5,1112) LI,LJ
C  READ(5,1112) ((NC(I,J),J=1,LJ),I=1,LI)
1112  FORMAT(24I3,/,24I3)
1114  FORMAT(4(F3.0,1X),F3.1)
C  DO 103 I = 1,4
C  MEAN = MEAN + SIGMAS(I)
103  SIGMA(I) = SQRT(SIGMAS(I))
C  MEAN = SQRT(MEAN) / CV
C
C  U1 MATRIX
C
C  DO 1002 L = 1,LI
C  N = 0
C  DO 1004 I = 1,LI
C  DO 1004 J = 1,LJ
C  N1 = NC(I,J)
C  IF (I .NE. L) GO TO 1008
C  DO 1006 K = 1,N1
C  N = N + 1
1006  U1(N,L) = 1
C  GO TO 1004
1008  DO 1010 K = 1,N1
C  N = N + 1
1010  U1(N,L) = 0
1004  CONTINUE
1002  CONTINUE
C  K = 0
C  DO 1040 I = 1,LI
C  DO 1040 J = 1,LJ
C  K = K + 1
1040  C(K) = U1(J,I)

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      K = 0
      DO 1043 J = 1,N
      DO 1043 I = 1,LI
      K = K + 1
1043  F(K) = U1(J,I)
      CALL GMPRD(C,F,E,N,LI,N)
      K = 0
      DO 1042 J = 1,N
      DO 1042 I = 1,N
      K = K + 1
1042  V1(I,J) = E(K)
C
C U2 MATRIX
C
      DO 1012 L = 1,LJ
      N = 0
      DO 1014 I = 1,LI
      DO 1014 J = 1,LJ
      N1 = NC(I,J)
      IF ( J - NE. L ) GO TO 1018
      DO 1016 K = 1,N1
      N = N + 1
1016  U2(N,L) = 1
      GO TO 1014
1018  DO 1020 K = 1,N1
      N = N + 1
1020  U2(N,L) = 0
1014  CONTINUE
1012  CONTINUE
      K = 0
      DO 1044 J = 1,LJ
      DO 1044 I = 1,N
      K = K + 1
1044  C(K) = U2(I,J)
      K = 0
      DO 1045 I = 1,N
      DO 1045 J = 1,LJ
      K = K + 1
1045  F(K) = U2(I,J)
      CALL GMPRD(C,F,E,N,LJ,N)
      K = 0
      DO 1046 J = 1,N
      DO 1046 I = 1,N
      K = K + 1
1046  V2(I,J) = E(K)
C
C U3 MATRIX
C
      JI = LI* LJ
      DO 1022 L = 1,JI
      N = 0
      IC = 0
      DO 1024 I = 1,LI
      DO 1024 J = 1,LJ
      IC = IC + 1
      N1 = NC(I,J)
      IF ( IC - NE. L ) GO TO 1028
      DO 1026 K = 1,N1
      N = N + 1
1026  U3(N,L) = 1
      GO TO 1024
1028  DO 1030 K = 1,N1
      N = N + 1
1030  U3(N,L) = 0
1024  CONTINUE
1022  CONTINUE
      K = 0
      DO 1048 J = 1,JI
      DO 1048 I = 1,N
      K = K + 1
1048  C(K) = U3(I,J)
      K = 0
      DO 1049 I = 1,N
      DO 1049 J = 1,JI
      K = K + 1
1049  F(K) = U3(I,J)
      CALL GMPRD(C,F,E,N,JI,N)
      K = 0
      DO 1050 J = 1,N
      DO 1050 I = 1,N
      K = K + 1
1050  V3(I,J) = E(K)

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C
C V4 MATRIX
C
      DO 1032 I = 1,N
      DO 1032 J = 1,N
      IF ( I - J ) 1034,1036,1034
1034  V4(I,J) = 0
      GO TO 1032
1036  V4(I,J) = 1
1032  CONTINUE
C
C X MATRIX
C
      DO 1052 I = 1,N
1052  X(I) = 1
C
      WRITE(6,7777)
7777  FORMAT('I15','ANOVA METHOD',I45,'MLE METHOD',I75,'MIVQUE METHOD',
      I7105,'I - MIVQUE METHOD',/)
      F1 = - N / 2.0
      F2 = 6.28318 * * ( F1 )
95  DO 14 I = 1,LI
C
C GENERATE A-EFFECT
C
      ALPHA(I) = NORM( ISEED1,SIGMA(1),MEANS )
14  CONTINUE
C
C GENERATE B-EFFECT
C
      DO 16 J = 1,LJ
      BETA(J) = NORM( ISEED2,SIGMA(2),MEANS )
16  CONTINUE
C
C GENERATE INTERACTION AB-EFFECT
C
      JI = 0
      DO 18 J = 1,LJ
      DO 20 I = 1,LI
      JI = JI + 1
      DINTRC(JI) = NORM( ISEED3,SIGMA(3),MEANS )
20  CCNTINUE
18  CCNTINUE
C
C GENERATE ERROR-EFFECT
C
      N = 0
      DO 24 I = 1,LI
      DO 26 J = 1,LJ
      N1 = NC(I,J)
      DO 28 K = 1,N1
      N = N + 1
      ERROR(N) = NORM( ISEED4,SIGMA(4),MEANS )
28  CONTINUE
26  CONTINUE
24  CONTINUE
C
C INITIALIZE VALUE
C
      DO 153 I = 1,N
      EFFECTA(I) = 0
      EFFECTB(I) = 0
      DINTER(I) = 0
153  CONTINUE
C
C MULTIPLY U1 BY ALPHA
C
      DO 92 I = 1,N
      DO 92 L = 1,LI
92  EFFECTA(I) = EFFECTA(I) + ( U1(I,L)*ALPHA(L) )
C
C MULTIPLY U2 BY BETA
C
      DO 113 I = 1,N
      DO 113 L = 1,LI
113  EFFECTB(I) = EFFECTB(I) + ( U2(I,L) * BETA(L) )
C
C MULTIPLY U3 BY INTRAC
C
      DO 123 I = 1,N
      DO 123 L = 1,JI
123  DINTER(I) = DINTER(I) + ( U3(I,L) * DINTRC(L) )

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C
C   ADDITION MATRIX TO GET Y(N) OR Y(I,J,K)
C
DO 133 I = 1,N
133 Y(I) = MEAN + EFECTA(I) + EFECTB(I) + DINTER(I) + ERROR(I)
    KK = 0
    DO 202 I = 1,LI
    DO 202 J = 1,LJ
    N1 = NC(I,J)
    DO 202 K = 1,N1
    KK = KK + 1
202   Y1(I,J,K) = Y(KK)
C
C.....C
C
C           =====>   THE ANOVA METHOD   <=====
C
C.....C
C
C   FIND TO
C
    TO = 0
    DO 210 I = 1,LI
    DO 210 J = 1,LJ
    N1 = NC(I,J)
    DO 210 K = 1,N1
210   TO = TO + Y1(I,J,K) ** 2
C
C   FIND TA
C
    TA = 0
    DO 213 I = 1,LI
    TTA(I) = 0
    NI(I) = 0
    DO 214 J = 1,LJ
    NI(I) = NI(I) + NC(I,J)
    N1 = NC(I,J)
    DO 217 K = 1,N1
217   TTA(I) = TTA(I) + Y1(I,J,K)
214   CONTINUE
213   TA = TA + ( TTA(I) ** 2 ) / NI(I)
C
C   FIND TB
C
    TB = 0
    DO 219 J = 1,LJ
    TTBJ(J) = 0
    NJ(J) = 0
    DO 221 I = 1,LI
    NJ(J) = NJ(J) + NC(I,J)
    N1 = NC(I,J)
    DO 223 K = 1,N1
223   TTBJ(J) = TTBJ(J) + Y1(I,J,K)
221   CONTINUE
219   TB = TB + ( TTBJ(J) ** 2 ) / NJ(J)
C
C   FIND TAB
C
    TAB = 0
    DO 224 I = 1,LI
    DO 224 J = 1,LJ
    TTAB(I,J) = 0
    N1 = NC(I,J)
    DO 226 K = 1,N1
226   TTAB(I,J) = TTAB(I,J) + Y1(I,J,K)
224   TAB = TAB + ( TTAB(I,J) ** 2 ) / NC(I,J)
C
C   FIND TU
C
    TTU = 0
    DO 228 I = 1,LI
    DO 228 J = 1,LJ
    N1 = NC(I,J)
    DO 235 K = 1,N1
235   TTU = TTU + Y1(I,J,K)
228   TU = (TTU ** 2) / N

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C
C   FIND K1,K2,K3,K4,K23
C
      AK1 = 0
      AK2 = 0
      AK3 = 0
      AK4 = 0
      AK23 = 0
C
C   FIND K1
C
      DO 232 I = 1,LI
232   AK1 = AK1 + NI(I) * * 2
C
C   FIND K2
C
      DO 234 J = 1,LJ
234   AK2 = AK2 + NJ(J) * * 2
C
C   FIND K3 & K23
C
      DO 236 I = 1,LI
      DUM = 0
      DO 238 J = 1,LJ
238   DUM = DUM + NC(I,J) * * 2
      AK23 = AK23 + DUM
236   AK3 = AK3 + DUM / NI(I)
C
C   FIND K4
C
      DO 240 J = 1,LJ
      DUM = 0
      DO 242 I = 1,LI
242   DUM = DUM + NC(I,J) * * 2
240   AK4 = AK4 + DUM / NJ(J)
      S1 = LI * LJ
      VE(1,4) = ( TO - TAB ) / ( N - S1 )
C
C   FIND MATRIX P
C
      P(1,1) = N - ( AK1 / N )
      P(1,2) = AK3 - ( AK2 / N )
      P(1,3) = AK3 - ( AK23 / N )
      P(2,1) = AK4 - ( AK1 / N )
      P(2,2) = N - ( AK2 / N )
      P(2,3) = AK4 - ( AK23 / N )
      P(3,1) = ( AK1 / N ) - AK4
      P(3,2) = ( AK2 / N ) - AK3
      P(3,3) = N - AK3 - AK4 + ( AK23 / N )
C
C   FIND P INVERT
C
      KK = 0
      DO 303 J = 1,3
      DO 303 I = 1,3
      KK = KK + 1
2303  C(KK) = P(I,J)
      CALL MINV( C,3,D,IRCN,ICOL )
      KK = 0
      DO 307 I = 1,3
      DO 307 J = 1,3
      KK = KK + 1
2307  P(I,J) = C(KK)
C
C   FIND OTHER MATRIX
C
      S(1) = TA - TU - ( LI - 1 ) * VE(1,4)
      S(2) = TB - TU - ( LJ - 1 ) * VE(1,4)
      S(3) = TAB - TA - TB + TU - ( S1 - LI - LJ + 1 ) * VE(1,4)
C
C   FIND VARIANCE COMPONENT
C
      DO 244 I = 1,3
      DUM = 0
      DO 246 J = 1,3
246   DUM = DUM + P(I,J) * S(J)
244   VE(1,I) = DUM
      DO 260 I = 1,4
      IF ( VE(1,I) .LE. 0 ) VE(1,I) = 0
260   CONTINUE

```



```

C.....C
C.....C
C      =====> THE MAXIMUM LIKELIHOOD METHOD <=====
C.....C
C.....C
C
DO 101 J = 1,4
101  VR(J) = VE(1,J)
      ND = 0
      INDEX = 0
      IA = 0
      EPS = 1.0E-7
2    DO 3 I=1,N
      DO 3 J=1,N
3    V(I,J) = VR(1)*V1(I,J)+VR(2)*V2(I,J)+VR(3)*V3(I,J)+ VR(4)*V4(I,J)
      K = 0
      DO 4 I=1,N
      DO 4 J=1,N
      K = K + 1
      F(K) = V(I,J)
      C(K) = V(J,I)
4    CALL MFGR(C,N,N,EPS,IRANK,IROW,ICOL)
      IF(N - IRANK) 5,6,5
5    WRITE(6,55)
55   FORMAT( T5,'RANK OF MATRIX IS NOT N' )
      GO TO 99
6    CALL MINV(F,N,C,IROW,ICOL)
      IF ( INDEX .EQ. 0 ) GO TO 90
      IF ( D .GT. 0) GO TO 450
      WRITE(6,452)
452  FORMAT( /,T5,'DETERMINANT < 0' )
      GO TO 99
450  CALL GMPRD(F,YSX,C,N,N,1)
      CALL GMPRD(YSX,C,F,1,N,1)
      FACT2 = EXP( - F(1) / 2 )
      FACT1 = F2 / SQRT(C)
      LIKH = FACT1 * FACT2
      IA = IA + 1
      INDEX = 0
      GO TO 220
90   K = 0
      DO 100 I = 1,N
      DO 100 J = 1,N
      K = K + 1
100  VIN(I,J) = F(K)
C
C ( X-TRANSPOST * V-INVERT ) 1*N
C
      CALL GMPRD(X,F,C,1,N,N)
C
C ( X-TRANSPOST * V-INVERT * Y ) 1*1
C
      CALL GMPRD(C,Y,E,1,N,1)
C
C ( X-TRANSPOST * V-INVERT * X ) 1*1
C
      CALL GMPRD(C,X,F,1,N,1)
C
      BET = E(1) / F(1)
      DO 102 I = 1,N
102  YSX(I) = Y(I) - X(I) * BET
      K = 0
      DO 104 J = 1,N
      DO 104 I = 1,N
      K = K + 1
104  C(K) = VIN(I,J)
      DO 142 II = 1,4
      GO TO ( 106,110,114,118 ) , II
106  K = 0
      DO 108 J = 1,N
      DO 108 I = 1,N
      K = K + 1
108  F(K) = V1(I,J)
      GO TO 122

```



```

110 K = 0
    DO 112 J = 1,N
    DO 112 I = 1,N
    K = K + 1
112 F(K) = V2(I,J)
    GO TO 122
114 K = 0
    DO 116 J = 1,N
    DO 116 I = 1,N
    K = K + 1
116 F(K) = V3(I,J)
    GO TO 122
118 K = 0
    DO 120 J = 1,N
    DO 120 I = 1,N
    K = K + 1
120 F(K) = V4(I,J)
C
C ( V-INVERT * V(I) ) N*N
C
122 CALL GMPRD(C,F,E,N,N)
    GO TO (124,128,132,136) , II
124 K = 0
    DO 126 J = 1,N
    DO 126 I = 1,N
    K = K + 1
126 VV1(I,J) = E(K)
    GO TO 140
128 K = 0
    DO 130 J = 1,N
    DO 130 I = 1,N
    K = K + 1
130 VV2(I,J) = E(K)
    GO TO 140
132 K = 0
    DO 134 J = 1,N
    DO 134 I = 1,N
    K = K + 1
134 VV3(I,J) = E(K)
    GO TO 140
136 K = 0
    DO 138 J = 1,N
    DO 138 I = 1,N
    K = K + 1
138 VV4(I,J) = E(K)
C
C ( V-INVERT * V(I) * V-INVERT ) N*N
C
140 CALL GMPRD(E,C,F,N,N,N)
C
C ( (Y-XBETA)-TRANSPCST * V-INVERT * V(I) * V-INVERT ) 1*N
C
    CALL GMPRD(Y,X,F,E,1,N,N)
C
C ( (Y-XBETA)-TRANSPST * V-INVERT * V(I) * V-INVERT * (Y-XBETA) ) 1*1
C
    CALL GMPRD(E,Y,X,F,1,N,1)
    S(II) = F(II)
142 CONTINUE
C
C TRANSFORM V(J) TO F
C
    DO 184 JJ = 1,4
    GO TO ( 144,148,152,156 ) , JJ
144 K = 0
    DO 146 J = 1,N
    DO 146 I = 1,N
    K = K + 1
146 F(K) = VV1(I,J)
    GO TO 160
148 K = 0
    DO 150 J = 1,N
    DO 150 I = 1,N
    K = K + 1
150 F(K) = VV2(I,J)
    GO TO 160
152 K = 0
    DO 154 J = 1,N
    DO 154 I = 1,N
    K = K + 1
154 F(K) = VV3(I,J)
    GO TO 160

```



```

154 K = 0
    CO 158 J = 1,N
    DO 158 I = 1,N
    K = K + 1
158 F(K) = VV4(I,J)
C
C TRANSFORM V(I) TO C
C
160 CO 182 II = 1,4
    GO TO ( 162,166,170,174 ) , II
162 K = 0
    DO 164 J = 1,N
    DO 164 I = 1,N
    K = K + 1
164 C(K) = VV1(I,J)
    GO TO 178
166 K = 0
    CO 168 J = 1,N
    DO 168 I = 1,N
    K = K + 1
168 C(K) = VV2(I,J)
    GO TO 178
170 K = 0
    DO 172 J = 1,N
    DO 172 I = 1,N
    K = K + 1
172 C(K) = VV3(I,J)
    GO TO 178
174 K = 0
    DO 176 J = 1,N
    DO 176 I = 1,N
    K = K + 1
176 C(K) = VV4(I,J)
C
C ( V-INVERT * V(J) * V-INVERT * V(I) ) N*N
C
178 CALL GMPDIC(F,E,N,N,N)
    K = 0
    DO 180 J = 1,N
    DO 180 I = 1,N
    K = K + 1
180 VJVI(I,J) = E(K)
C
C TR( V-INVERT * V(J) * V-INVERT * V(I) )
C
    CALL TRACE(VJVI,N,SUM)
    TR(JJ,II) = SUM
182 CCNTINUE
184 CCNTINUE
C
    K = 0
    DO 196 J = 1,4
    F(J) = S(J)
    DO 194 I = 1,4
    K = K + 1
    E(K) = TR(I,J)
194 C(K) = TR(I,J)
196 CCNTINUE
    L = 4
    K = 0
    CALL MFGR(E,L,L,EPS,IRANK,IROW,ICOL)
    IF ( IRANK - L ) 231,200,231
231 WRITE(6,1111) IRANK
1111 FORMAT(T5,'RANK = ',I4)
    GO TO 99
200 CALL MINV(C,L,D,IROW,ICOL)
    CALL GMPRC(C,F,E,L,L,I)
    DO 212 J = 1,L
212 VR(J) = E(J)
    DO 214 J = 1,4
    IF ( VR(IJ) .LT. 0 ) VR(J) = 0
214 CCNTINUE
    INDEX = 1
220 IF ( INDEX .EQ. 1 ) GO TO 2
    IF ( IA .EQ. 1 ) GO TO 454
    IF ( MAX .GE. LIKH ) GO TO 456
454 MAX = LIKH
C
C VARIANCE COMPONENT
C
    DO 458 J = 1,4
458 VE(2,J) = VR(J)
    IE = 0
    GO TO 2
456 IE = IE + 1
    IF ( IE .LT. 2 ) GO TO 2

```



```

C
C ..... C
C ..... C
C =====> THE MINVQUE & THE I-MINVQUE METHOD <===== C
C ..... C
C ..... C
DO 300 J = 1,4
300 VR(J) = VE(1,J)
ND = 0
302 DO 304 I=1,N
DO 304 J=1,N
304 V(I,J) = VR(1)*V1(I,J)+VR(2)*V2(I,J)+VR(3)*V3(I,J)+ VR(4)*V4(I,J)
K = 0
DO 306 I=1,N
DO 306 J=1,N
K = K + 1
F(K) = V(J,I)
306 C(K) = V(J,1)
CALL MFRG(C,N,N,EPS,IRANK,IROW,ICOL)
IF(N - IRANK) 308,310,308
308 WRITE(6,305)
305 FORMAT( '5,*RANK OF MATRIX IS NOT N' )
GO TO 99
310 CALL MINV(F,N,D,IROW,ICOL)
K = 0
DO 312 I = 1,N
DO 312 J = 1,N
K = K + 1
312 VIN(I,J) = F(K)
C
C ( X-TRANSPST * V-INVERT ) I*N
C
CALL GMPRD(X,F,C,1,N,N)
C
C ( V-INVERT * X ) N*1
C
CALL GMPRD(F,X,E,N,N,1)
C
C ( X-TRANSPST * V-INVERT * X ) I*I
C
CALL GMPRD(C,X,F,1,N,1)
C
C ( X-TRANSPST * V-INVERT * X ) -INVERT
C
XVXI(1) = 1 / F(1)
C
C ( V-INVERT * X * (X-T*V-I*X)-INVERT ) N*1
C
CALL GMPRD(E,XVXI,F,N,1,1)
C
C ( V-INVERT * X * (X-T * V-I *X)-INVERT * X-TRANSPST * V-INVERT
C
CALL GMPRD(F,C,E,N,1,N)
C
C MATRIX Q (N*N)
C
K = 0
DO 314 J = 1,N
DO 314 I = 1,N
K = K + 1
314 VJVI(I,J) = E(K)
DO 316 I = 1,N
DO 316 J = 1,N
316 Q(I,J) = VIN(I,J) - VJVI(I,J)
C
C
K = 0
DO 318 J = 1,N
DO 318 I = 1,N
K = K + 1
318 C(K) = Q(I,J)
DO 356 II = 1,4
GO TO ( 320,324,328,332 ) , II
320 K = 0
DO 322 J = 1,N
DO 322 I = 1,N
K = K + 1
322 F(K) = V1(I,J)
GO TO 336

```



```

324 K = 0
DO 326 J = 1,N
CO 326 I = 1,N
K = K + 1
326 F(K) = V2(I,J)
GO TO 336
328 K = 0
DO 330 J = 1,N
DO 330 I = 1,N
K = K + 1
330 F(K) = V3(I,J)
GO TO 336
332 K = 0
DO 334 J = 1,N
DO 334 I = 1,N
K = K + 1
334 F(K) = V4(I,J)
C
C ( O * V(I) ) N*N
C
336 CALL GMPRD(C,F,E,N,N,N)
C
GO TO (338,342,346,350) , II
338 K = 0
DO 340 J = 1,N
CO 340 I = 1,N
K = K + 1
340 VV1(I,J) = E(K)
GO TO 354
342 K = 0
DO 344 J = 1,N
DO 344 I = 1,N
K = K + 1
344 VV2(I,J) = E(K)
GO TO 354
346 K = 0
DO 348 J = 1,N
DO 348 I = 1,N
K = K + 1
348 VV3(I,J) = E(K)
GO TO 354
350 K = 0
DO 352 J = 1,N
DO 352 I = 1,N
K = K + 1
352 VV4(I,J) = E(K)
C
C ( O * V(I) * Q ) N*N
C
354 CALL GMPRD(E,C,F,N,N,N)
C
C ( Y-TRANSPOST * Q * V(I) * C ) 1*N
C
CALL GMPRD(Y,F,E,1,N,N)
C
C ( Y-TRANSPOST * Q * V(I) * Q * Y ) 1*1
C
CALL GMPRD(E,Y,F,1,N,1)
S(II) = F(1)
356 CONTINUE
C
C TRANSFORM V(J) TO F
C
DO 398 JJ = 1,4
GO TO ( 358,362,366,370 ) , JJ
358 K = 0
DO 360 J = 1,N
DO 360 I = 1,N
K = K + 1
360 F(K) = VV1(I,J)
GO TO 374
362 K = 0
DO 364 J = 1,N
DO 364 I = 1,N
K = K + 1
364 F(K) = VV2(I,J)
GO TO 374

```



```

366 K = 0
    DO 368 J = 1,N
    DO 368 I = 1,N
    K = K + 1
368 F(K) = VV3(I,J)
    GO TO 374
370 K = 0
    DO 372 J = 1,N
    DO 372 I = 1,N
    K = K + 1
372 F(K) = VV4(I,J)
C
C TRANSFORM V(I) TO C
C
374 DO 396 II = 1,4
    GO TO ( 376,380,384,388 ), II
376 K = 0
    DO 378 J = 1,N
    DO 378 I = 1,N
    K = K + 1
378 C(K) = VV1(I,J)
    GO TO 392
380 K = 0
    DO 382 J = 1,N
    DO 382 I = 1,N
    K = K + 1
382 C(K) = VV2(I,J)
    GO TO 392
384 K = 0
    DO 386 J = 1,N
    DO 386 I = 1,N
    K = K + 1
386 C(K) = VV3(I,J)
    GO TO 392
388 K = 0
    DO 390 J = 1,N
    DO 390 I = 1,N
    K = K + 1
390 C(K) = VV4(I,J)
C
C ( Q * V(I) * Q * V(J) ) N*N
C
392 CALL GMPRD(F,C,E,N,N,N)
    K = 0
    DO 394 J = 1,N
    DO 394 I = 1,N
    K = K + 1
394 VJVI(I,J) = E(K)
C
C TR( Q * V(J) * Q * V(I) )
C
    CALL TRACE(VJVI,N,SUM)
    TR(JJ,II) = SUM
396 CONTINUE
398 CONTINUE
    K = 0
    DO 400 J = 1,4
    DO 400 I = 1,4
    K = K + 1
    C(K) = TR(I,J)
400 F(K) = TR(I,J)
    CALL MFGR(F,4,4,EPS,IRANK,IRQW,ICOL)
    IF ( IRANK - 4 ) 99,402,99
402 CALL MINV(C,4,C,IRQW,ICEL )
    CALL GMPRD(C,S,E,4,4,1)
    DO 403 J = 1,4
    IF ( E(J) .LT. 0 ) E(J) = 0
403 CONTINUE

```



```

      IF ( ND .NE. 0 ) GO TO 404
C
C   VARIANCE COMPONENT BY MINQUE METHOD
C
      DO 401 J = 1,4
401  VE(3,J) = E(J)
C
C   VARIANCE COMPONENT BY I-MINQUE METHOD
C
404  DO 405 J = 1,4
405  VE(4,J) = E(J)
      DO 406 J = 1,4
      IF ( ABS(VE(4,J) - VR(J)) .GT. 0.05 ) GO TO 418
406  CONTINUE
      KOUNT1 = KOUNT1 + 1
      WRITE(6,333) KOUNT1,((VE(I,J),J=1,4),I=1,4)
333  FORMAT(T1,I4,16(F7.2,1X) )
      GO TO 430
418  ND = ND + 1
      IF ( ND .GE. 20 ) GO TO 99
      DO 420 J = 1,4
420  VR(J) = VE(4,J)
      GO TO 302
C
C   CUMULATIVE STATISTICS
C
430  DO 432 I = 1,4
      DO 432 J = 1,4
      SS(I,J) = SS(I,J) + ( (VE(I,J)-SIGMAS(J)) ** 2)
432  CCNTINUE
      IF ( KOUNT1 .GE. 200 ) GO TO 434
      GO TO 99
434  DO 436 I = 1,4
      DO 436 J = 1,4
      MSE(I,J) = SS(I,J) / KOUNT1
436  SMSE(I) = SMSE(I) + MSE(I,J)
      DO 438 I = 1,4
438  WRITE(6,440) I,(MSE(I,J),J=1,4),SMSE(I)
440  FORMAT(T2,'MSE OF METHOD ',I1,' = ',5(F20.4,1X) )
      DO 442 I = 1,4
442  WRITE(6,446) (SS(I,J),J=1,4)
446  FORMAT(T1,4(F20.5,1X))
      STOP
      END

```

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```

C   RECODE MATRIX
C
    DO 65 I=1,N
    IK = NK + I
    HOLD = A(IK)
    IJ = I - N
    DC 65 J =1,N
    IJ = IJ + N
    IF (I-K) 60,65,60
60   IF (J-K) 62,65,62
62   KJ = IJ -I + K
    A(IJ) = HOLD * A(KJ) +A(IJ)
65   CCNTINUE
C
C   DIVIDED ROW BY PIVOT
C
    KJ = K, - N
    DC 75 J=1,N
    KJ = KJ + N
    IF(J-K) 70,75,70
70   A(KJ) = A(KJ) / BIGA
75   CCNTINUE
C
C   PRODUCT OF PIVOT
C
    D = D * BIGA
C
C   REPLACE PIVOT BY RECIPCCAL
C
    A(KK) = 1.0 / BIGA
80   CCNTINUE
C
C   FINAL ROW AND COLUMN INTERCHANGE
C
    K = N
100  K = (K-1)
    IF (K) 150,150,105
105  I = L(K)
    IF (I-K) 120,120,108
108  JQ = N * (K-1)
    JR = N * (I-1)
    DC 110 J=1,N
    JK = JQ + J
    HCLD = A(JK)
    JI = JR + J
    A(JK) = -A(JI)
110  A(JI) = HOLD
120  J = M(K)
    IF(J-K) 100,100,125
125  KI = K - N
    DC 130 I=1,N
    KI =KI + N
    HCLD = A(KI)
    JI = KI - K + J
    A(KI) = - A(JI)
130  A(JI) = HOLD
    GO TO 100
150  RETURN
    END

```



```

C
C.....
C.....
C.....          SUBROUTINE MFGR          .....
C.....          =====          .....
C.....          FIND RANK OF MATRIX A    .....
C.....
C.....
C
      SUBROUTINE MFGR(A,M,N,EPS,IRANK,IROW,ICOL)
      DIMENSION A(1),IROW(1),ICOL(1)
C
      DOUBLE PRECISION A,PIV,HOLD,SAVE
      MN = N * M
      DO 100 J = 1,MN
100    CONTINUE
      IF(M) 2,2,1
1    IF(N) 2,2,4
2    IFRANK = -1
3    RETURN
C
C    INITIALIZE COLUMN INDEX VECTOR
C    SEARCH FIRST PIVOT ELEMENT
C
4    IFRANK = 0
      PIV = 0.
      JJ = 0
      DO 6 J=1,N
      ICOL(J) = J
      DO 6 I=1,M
      JJ = JJ + 1
      HOLD = A(JJ)
5    IF( ABS(PIV) - ABS(HOLD)) 5,6,6
      PIV = HOLD
      IF = I
      IC = J
      CCNTINUE
6
C
C    INITIALIZE ROW INDEX VECTOR
C
      DO 7 I =1,M
7    IROW(I) = I
C
C    SET UP INTERNAL TOLERANCE
C
      TOL = ABS(EPS * PIV)
C
C    INITIALIZE ELEMENT LOOP
C
      NM = N * M
      DO 49 NCOL = 1,NM,M
C
C    TEST FOR FEASIBILITY OF PIVOT ELEMENT
C
8    IF( ABS(PIV) - TOL) 20,20,6
C
C    UPDATE RANK
C
9    IFRANK = IFRANK + 1
C
C    INTERCHANGE ROWS IF NECESSARY
C
      JJ = IR - IFRANK
      IF(JJ) 12,12,10
10   DO 11 J=IFRANK,NM,M
      I = J + JJ
      SAVE = A(J)
      A(J) = A(I)
11   A(I) = SAVE
C
C    UPDATE ROW INDEX VECTOR
C
      JJ = IROW(IR)
      IROW(IR) = IROW(IFRANK)
      IROW(IFRANK) = JJ
C
C    INTERCHANGE COLUMN IF NECESSARY
C
12   JJ = (IC - IFRANK) * M
      IF(JJ) 15,15,13
13   KK = NCOL

```



```

DC 14 J=1,M
I = KK + JJ
SAVE = A(KK)
A(KK) = A(I)
KK = KK - 1
A(I) = SAVE
14
C
C UPDATE COLUMN INDEX VECTOR
C
JJ = ICCL(IC)
ICCL(IC) = ICOL(IRANK)
ICCL(IRANK) = JJ
15
KK = IRANK + 1
MM = IRANK - M
LL = NCOL + MM
C
C TEST FOR LAST ROW
C
IF (MM) 16,25,25
C
C TRANSFORM CURRENT SUBMATRIX AND SEARCH NEXT PIVOT
C
16
JJ = LL
SAVE = PIV
PIV = 0.
DO 39 J=KK,M
JJ = JJ + 1
HCLD = A(JJ) / SAVE
A(JJ) = HCLD
L = J - IRANK
C
C TEST FOR LAST COLUMN
C
IF(IRANK - N) 17,39,39
17
II = JJ
DC 19 I=KK,N
II = II + M
MM = II - L
A(II) = A(II) - HCLD * A(MM)
IF ( ABS(A(II)) - ABS(PIV) ) 19,19,18
18
PIV = A(II)
IF = J
IC = I
19
CCONTINUE
39
CCONTINUE
49
CCONTINUE
C
C SET UP MATRIX EXPRESSION ROW DEPENDENCIES
C
20
IF ( IRANK - 1 ) 3,25,21
21
IR = LL
DO 24 J = 2,IRANK
II = J - 1
IR = IR - M
JJ = LL
DO 23 I = KK,M
HOLD = 0.
JJ = JJ + 1
MM = JJ
IC = IR
DC 22 L = 1,II
HCLD = HCLD + A(MM) * A(IC)
IC = IC - 1
22
MM = MM - M
23
A(MM) = A(MM) - HOLD
24
CCONTINUE

```



```

C
C TEST FOR COLUMN REGULARITY
C
25 IF ( N - IRANK ) 3,3,26
C
C SET UP MATRIX EXPRESSING BASIC VARIABLES IN TERM OF FREE
C PARAMETERS ( HOMOGENECUS SCLUSION )
C
26 IR = LL
   KK = LL + M
   DC 30 J = 1,IRANK
   DC 29 I = KK,NM,M
   JJ = IR
   LL = I
   HCLD = 0.
27 II = J
   II = II - 1
   IF ( II ) 29,29,28
28 HOLD = HOLD - A(JJ) * A(LL)
   JJ = JJ - M
   LL = LL - 1
   GC TO 27
29 A(LL) = ( HOLD - A(LL) ) / A(JJ)
30 IR = IR - 1
   RETURN
   END

```

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```

C
C.....
C.....
C.....          SUBROUTINE TRACE          .....
C.....          =====          .....
C.....          FIND TRACE OF MATRIX A    .....
C.....
C.....
C.....
C
C      SUBROUTINE TRACE(A,N,SUM)
C      DIMENSION A(30,30)
C      DOUBLE PRECISION A,SUM
C      SUM = 0.0
C      DO 10 I = 1,N
C      DO 10 J = 1,N
C      IF ( I - J ) 10,20,10
20      SUM = SUM + A(I,J)
10      CCNTINUE
      RETURN
      END

```

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```

C
C.....
C.....
C.....          SUBROUTINE RANDU          .....
C.....          =====          .....
C.....          FOR GENERATE RANDOM NUMBER WITH UNIFORM DISTRIBUTION .....
C.....
C.....
C
C          SUBROUTINE RANDU( IX,IY,YFL )
C          IY = IX * 65539
C          IF (IY) 5,6,6
5  IY = IY + 2147483647 + 1
6  YFL = IY
C          YFL = YFL / 2147483647
C          RETURN
C          END

```

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## ประวัติผู้เขียน

นางสาวยุพิน คำเหม็ง เกิดเมื่อวันที่ 14 มิถุนายน พ.ศ. 2503 ที่จังหวัด  
อุดรธานี สำเร็จการศึกษาปริญญาตรี ศึกษาศาสตร์บัณฑิต (ลัทธิ) จากมหาวิทยาลัยเชียงใหม่  
เมื่อปีการศึกษา 2525 และเข้าศึกษาต่อระดับปริญญาโทในภาควิชาลัทธิ จุฬาลงกรณ์มหาวิทยาลัย  
ปีการศึกษา 2526 ปัจจุบันทำงานอยู่ที่กองการสอบ สำนักงาน ก.พ.



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